MA 314 Homework 20:

## 1. Mortar

- (1) Read Bonahon Sections 8.1 8.3
- (2) Read problems 8.5 and 8.6 (pages 224 225) and try your hand at proving them.

## 2. BRICKS

- (1) Let  $X = \mathbb{R}^2 \{0\}$  and let  $\Gamma$  be the group of diffeomorphisms of X generated by  $\gamma(x, y) = (2x, y/2)$ . (That is,  $\Gamma$  consists of all functions obtained by composing  $\gamma$  with itself some finite number of times.)
  - (a) Show that  $\Gamma$  acts freely and discontinuously on *X*.
  - (b) Use a computer to draw the circle  $x^2 + (y-2)^2 = 1$  and the image of that circle under  $\gamma$  and  $\gamma^2$ .
  - (c) Show that the quotient pseudo-metric  $\overline{d}$  on  $X/\Gamma$  is not a metric.