## Calculus II: Spring 2018 Homework

## Due March 21, 6pm

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## Some thoughts and advice:

- $\bullet$  You should expect to spend at least 1 2 hours on problem sets. A lot of practice problem-solving is essential to understand the material and skills covered in class. Be organised and do not leave problem sets until the last-minute. Instead, get a good start on the problems as soon as possible.
- When approaching a problem think about the following: do you understand the words used to state the problem? what is the problem asking you to do? can you restate the problem in your own words? have you seen a similar problem worked out in class? is there a similar problem worked out in the textbook? what results/skills did you see in class that might be related to the problem?

If you are stuck for inspiration, use the course piazza forum (accessible via the course Canvas site), come to office hours, or send me an email. However, don't just ask for the solution - provide your thought process, the difficulties you are having, and ask a coherent question in complete English sentences. Remember the 3RA approach to asking questions outlined in the course syllabus.

- Form study groups get together and work through problem sets. This will make your life easier! You can use piazza to arrange meet-ups. However, you must write your solutions on your own and in your own words.
- If you would like more practice then there are (hundreds of) problems in the supplementary course textbooks mentioned in the syllabus, or you can check out khanacademy.org.
- You are not allowed to use any additional resources. If you are concerned then please ask.
- 1. Each of the following functions is one-to-one. Determine the rule  $x \mapsto f^{-1}(x)$  defining the inverse function. Determine the domain and codomain of  $f^{-1}$ .

(a) 
$$f(x) = 3x + 7, -10 \le x \le 5.$$

(b) 
$$f(x) = 5x^3 - 1, -\infty < x < \infty.$$

(c) 
$$f(x) = -3x^2 + \pi$$
,  $-2 < x < -1$ .

(d) 
$$f(x) = \frac{10}{2-9x}$$
,  $1 < x < 5$ .

(e) 
$$f(x) = \frac{x}{x^2 - 3x + 2}, x > 2.$$

- 2. Determine a, b so that the function  $f(x) = \frac{x+1}{x^2+ax+b}$ , -2 < x < 2, is one-to-one. (Note: there are infinitely many choices for a, b)
- 3. True/False. No justification required.
  - (a) If f(x), g(x),  $a \le x \le b$ , are both one-to-one then (f+g)(x),  $a \le x \le b$ , is one-to-one.
  - (b) If f(x) is one-to-one then f(x) is strictly increasing.
  - (c) If f(x) is a function with inverse  $f^{-1}(x) = 2x + 1$ ,  $2 \le x \le 3$ , then f(x) is one-to-one.
  - (d) Every function of the form  $f(x) = x^3 + cx + d$ , where c, d are constants, is one-to-one.