



TRIGONOMETRIC IDENTITIES

THE ESSENTIALS

- $\sin^2(x) + \cos^2(x) = 1$
- $\sin(2x) = 2 \sin(x) \cos(x)$
- $\cos(2x) = \cos^2(x) - \sin^2(x)$

USEFUL FOR INTEGRATION

Using the above identities you can deduce the following identities:

- $1 + \tan^2(x) = \sec^2(x)$
- $1 + \cot^2(x) = \csc^2(x)$
- $\sin^2(x) = \frac{1}{2} (1 - \cos(2x))$
- $\cos^2(x) = \frac{1}{2} (1 + \cos(2x))$

THE EXTRAS

The following identities may be useful:

- $\cos(x \pm y) = \cos(x) \cos(y) \mp \sin(x) \sin(y)$
- $\sin(x \pm y) = \sin(x) \cos(y) \pm \sin(y) \cos(x)$
- $\cos(x) \cos(y) = \frac{1}{2} (\cos(x + y) + \cos(x - y))$
- $\sin(x) \sin(y) = \frac{1}{2} (\cos(x - y) - \cos(x + y))$