

PRACTICE FINAL

Disclaimer: This Practice Final consists of problems of a similar difficulty as will be on the actual final. However, **problems on the actual final may or may not be quite different in nature, and may or may not focus on different course material.** However, the actual final will have a similar format: one true/false problem, one short-answer problem, three long-answer problems.

1. True/False (no justification required)

(a) The function $f(x) = |x|$ does not possess an antiderivative.

(b) The formula $\int_0^x f''(x)dx = f'(x) - f'(0)$ holds.

(c) If $F(x)$ is an antiderivative of $f(x)$ then $F'(x) = f(x)$.

(d) $\int e^{x^2} dx = \frac{e^{x^2}}{2x} + C$

(e) $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{\pi \sin(\pi k/n)}{n} = 2$

2. Compute the indefinite integral.

(a)

$$\int x \cos(\pi x + e) dx$$

(b)

$$\int \frac{1}{x \ln(x)} dx$$

3. Determine the area bounded between the curves $y = 1 - x$ and $y = 1 - x^2$.

4. Consider the function

$$f(x) = \int_0^{x^2} \sin(t^2) dt$$

(a) Compute $f'(x)$.

(b) Determine the equation of the tangent line to the curve $y = f(x)$ at $x = \pi$.

5. Let $f(x) = 1/\sqrt{x-1}$, defined when $x > 1$.

(a) Let $1 < t < 5$. Compute $A(t) = \int_t^5 f(x) dx$.

(b) Compute $\lim_{t \rightarrow 1^+} A(t)$.

(c) True/False: the area bounded below $y = f(x)$, $1 < x \leq 5$, is $\lim_{t \rightarrow 1^+} A(t)$. **Justify your answer.**

