Topics in Algebra

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Final Project

Goal: The goal of this project is to demonstrate both your ability to teach yourself advanced mathematics and your ability to communicate the motivation and high-level technical methods to peers.

Format: The project consists of two parts:

- (1) A short paper (approx 5-6 pages) describing a specific infinite, finitely generated group (everyone but Sam) or type of group (Sam) and its algebraic and geometric properties.
- (2) A short (approx 5 minute) recorded lecture, to be shared with your classmates, describing the group and one or two of its geometric properties.

Requirements:

- (1) The project must rely mostly on one or both of the course texts.
- (2) The paper must reference two research papers on the topic. You need to have read the papers to get a sense of their methods, but you do not need to understand all (or even most) of the papers.
- (3) You must cite all sources you rely on, whether or not you explicitly quote from them. You should use in-text references to a bibliography at the end.
- (4) You should include figures (which may be hand-drawn) to illustrate your points.
- (5) The paper should be properly typed in LATEX, including with a proper bibliography and all.
- (6) The paper should clearly explain the definitions, provide some illustrative examples, state some theorems, and in **very few** sentences summarize the general method of proof of the theorems.
- (7) The paper should conclude with 2 or 3 "digging deeper" questions for further study.
- (8) The recorded lecture should use either pre-prepared slides or live-writing on a tablet computer. It should answer the question, "What was your project about and what makes it interesting?"