## Fall 2017/MA 397 HW 2: Paths!

Remember that, although you are encouraged to work together, all of your write-ups must be your own (no copying someone else's solution - not even with minor wording changes.) List the names of everyone you worked with on the HW! You are encouraged to not look online for solutions - your time is better spent wrestling with the proof yourself or getting help from the professor, than squandering it online.

## 1. Reading

- Read Pages 6 30 of the text. (You may skip unassigned problems)
- Memorize the definition of chromatic number, path, cycle, planar graph, subgraph, connected, graph isomorphism, girth, Petersen graph, vertex transitive, walk, trail, cut edge, cut vertex, induced subgraph, Eulerian circuit, maximum, maximal.
- Study the proofs of Lemma 1.2.15, 1.2.18, 1.2.25, 1.2.26, 1.2.27. We'll go over some of these in class.

## 2. To do

## Problems:

- (1) 1.1.13 (Remember that a *k*-tuple in  $\{0,1\}$  means a vector  $(x_1,...,x_k)$  with each  $x_i \in \{0,1\}$ .) The minimal length of a path from a vertex *x* to a vertex *y* in *G* is called the **Hamming distance** from *x* to *y*. This graph and distance function are important in information theory.
- (2) 1.1.18, 1.1.24 (practice with graph isomorphisms)
- (3) 1.1.26. (Hint: The fact that the graph has girth 4 means that there are no triangles. In particular, whenever  $\{a,b\}$  and  $\{b,c\}$  are edges with  $b \neq c$ , then  $\{a,c\}$  is not an edge of the graph.)
- (4) 1.2.2 (practice with definitions)
- (5) 1.2.6 (practice with definitions)
- (6) 1.2.8
- (7) 1.2.12 (If you know how to program, you might write a computer program to do this!)
- (8) 1.2.25
- (9) 1.2.40 (Practice with paths)