Here are some suggestions for what and how to study:

- (1) Know the definitions on the website. Any other definitions that you need will be given to you.
- (2) When you write a proof, focus on getting the organization clear and correct. If you have to skip some steps or make an assumption that you don't know how to prove, clearly state that that is what you are doing.
- (3) Know the theorems we've proved in class and the more significant theorems from the homework.
- (4) Don't try to memorize proofs. Instead remember the structure of the proof (proof by contradiction, proof of uniqueness, element argument, etc.) and two or three key steps of the proof. Then at the exam recreate the proof.
- (5) At the exam, leave time to write up a nicely written version of each proof. You should have enough time to sketch your ideas out on scratch paper before writing a final version of the proof.
- (6) Here are some results you should be especially sure to know how to prove. You should also think about ways these problems might be varied. And you should study other problems too.
 - (a) The compositions of injections/surjections/bijections is a an injection/surjection/bijection.
 - (b) A function $f: X \to Y$ is a bijection if and only if there is a function $f^{-1}: X \to Y$ such that $f \circ f^{-1}(y) = y$ for all $y \in Y$ and $f^{-1} \circ f(x) = x$ for all $x \in X$.
 - (c) Basic proofs by induction (see text, homework, and class notes)
 - (d) Euler's theorem for planar graphs: If G is a finite, planar, non-empty, connected graph with V(G) vertices, E(G) edges, and F(G) faces, then V(G) E(G) + F(G) = 2.
 - (e) The Well-Ordering Principle
 - (f) Every integer greater than one is a multiple of a prime number.
 - (g) Every fraction can be written in lowest terms.
 - (h) Chinese Remainder Theorem
 - (i) If *P* is a convex polygon with $n \ge 3$ sides, then *P* can be tiled by (n-2) triangles.
 - (j) The cardinality of a finite set is well-defined (Theorem 8.1.3)

- (k) Removing an element from a finite set reduces the cardinality by 1 (Theorem 8.1.4)
- (1) The cardinalities of finite sets are additive under disjoint union (Theorem 8.1.6 and Exercise 8.1.8)
- (m) cardinalities of finite sets are multiplicative under Cartesian products (Theorem 8.1.10)
- (n) All of the parts of Exercise 8.2.3
- (o) The basic idea of the proof of Exercise 8.2.5.
- (p) Theorem 8.2.6 (subsets of countable sets are countable)
- (q) card $\mathbb{N} \times \mathbb{N} =$ card \mathbb{N} (the Cantor Snake)
- (r) The rationals are countable
- (s) \mathbb{R} is uncountable
- (t) For every set *X*, card *X* < card $\mathscr{P}(X)$.