Mathematics 231

Lecture 6 Liam O'Brien

Announcements

Reading

 Today 	M&M 2.1	83-94
	M&M 2.2	101-104
 Next class 	M&M 2.3	108-121

Methods to Check Normality

- There are many methods that have been developed to check normality.
- Some methods are more sensitive to departures from normality than others.
- Histograms and boxplots provide a graphical method for checking the basic shape and spread of a distribution.
- One more sensitive and common method for checking the assumption of normality is called a normal quantile plot.

Normal Quantile Plots

- Cannot be constructed by hand, but Stata can do them.
- If you were to construct them by hand, you would first order the data.
- Then you would construct a z-score for each point.
- Plot the ordered *x* versus the z-scores.
- If the data are normal, then they will fall on a straight line.











Linear Relationships and Correlation

- Distinction between categorical and quantitative variables
- Linear relationship between two variables
- Scatter plot
- Correlation



Positive and Negative Association

- Positive Association: High values of one variable tend to accompany high values of the other variable, and low values of one variable tend to accompany low values of the other variable.
- **Negative Association:** High values of one variable tend to accompany low values of the other variable and vice versa.
- What type of association do we see in the immunization data?



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Linear Relationship

- Do the immunization data show a linear relationship?
- Could you imagine easily fitting a straight line to these data?

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Do you think that line would fit well?











Correlation Coefficient

- Correlation Coefficient, denoted as *r* (or ρ), measures the strength of *linear* association between two quantitative variables.
- Properties:
 - *r* measures linear association
 - r always falls between -1 and +1
 - r = 1 or -1 only if observations lie exactly along a straight line



Suppose we have a list of *n* pairs of observations:

 $(x_1, y_1), (x_2, y_2), (x_3, y_3), \dots, (x_n y_n)$

Correlation of X and Y is given by,

$$r = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{x_i - \overline{x}}{s_x} \right) \left(\frac{y_i - \overline{y}}{s_y} \right)$$

where s_x and s_y are the SDs of X and Y.

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Correlation Coefficient

- Additional Properties:
 - Sign if *r* indicates whether there is positive (+) or negative (-) association.
 - Absolute value of *r* measures the strength of the linear relationship.
 - *r* is unaltered by changes in the units of measurement of X and/or Y.
 - *r* has no units of measurement, e.g., r = 0.8 is not twice as strong as r = 0.4.



Example: Mortality	
 Under 5-mortality rate per 1,000 live births versus percent immunized against DPT. correlate immune mortality (obs=20) 	
immune mortal~y	
immune 1.0000 mortality -0.8291 1.0000	
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