# Mathematics 231

Lecture 2 Liam O'Brien

# Announcements

# Reading Today M&M 1.1 6-16 Next class M&M 1.2 30-44

# **Describing Data**

Variables: Categorical versus quantitative
Displaying Distributions with graphs
Bar graphs, pie charts, histograms, stem-and-leaf plots

Skewness

## Variables and Distributions

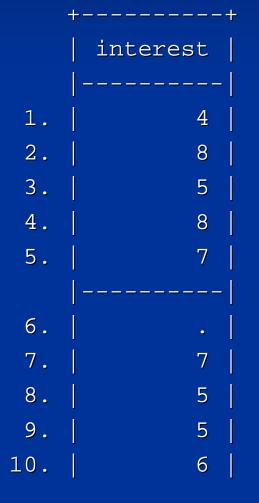
Variable: Any particular characteristic that can take on different "values" for each individual.

**Examples**: Age, gender, GPA, major

- Categorical variable: Places individuals into one of several groups or categories.
- Quantitative variable: Takes numerical values for which arithmetic operations are meaningful.

# **Example:** Survey Question

What is your interest in this course?



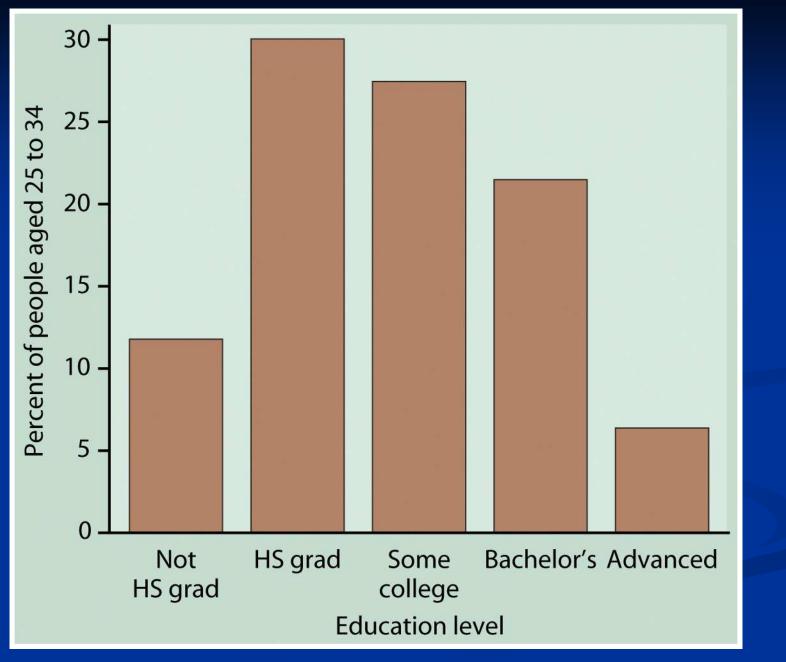
## **Distribution of a Variable**

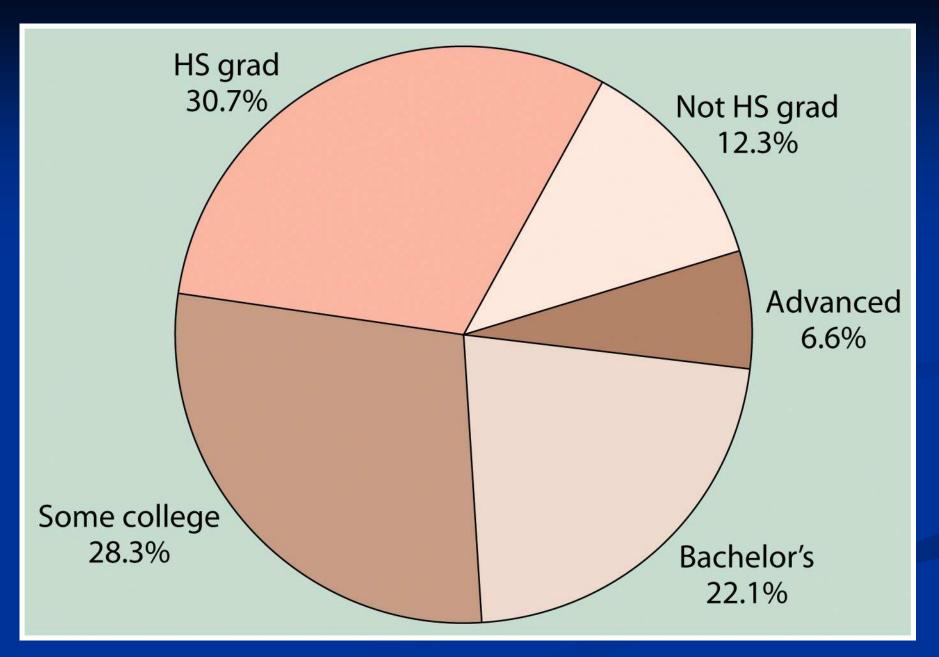
- **Distribution:** Describes what values a variable takes on, and how frequently these values occur.
- The distribution of a variable can be described through both graphics and numerical summaries.
- The three most used characteristics are shape, center (or location), and spread (or variability).
- Shape: A picture is worth a thousand words.

# **Graphs for Categorical Data**

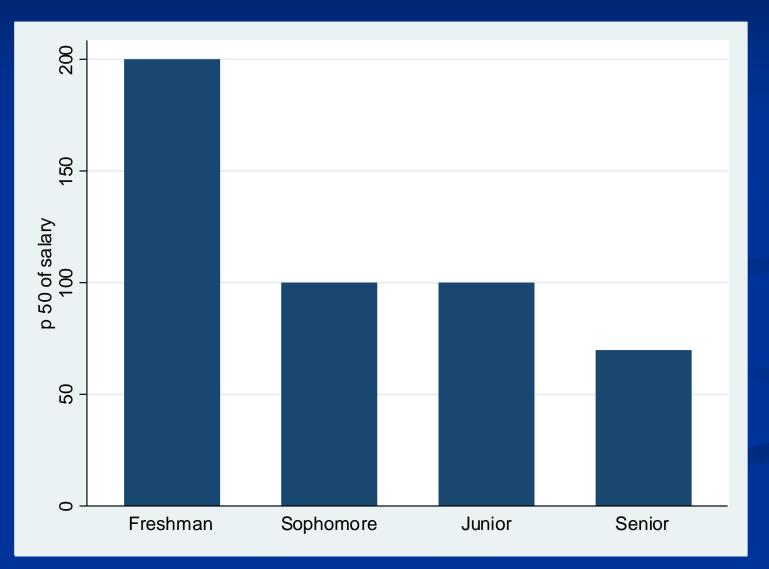
 Bar graphs: Display count/percentage of individuals in each category.

Pie charts: Display percentages of individuals in each category as "wedges" in a "pie."





# Bar Chart of Mediam Income by Class



# **Graphs for Quantitative Data**

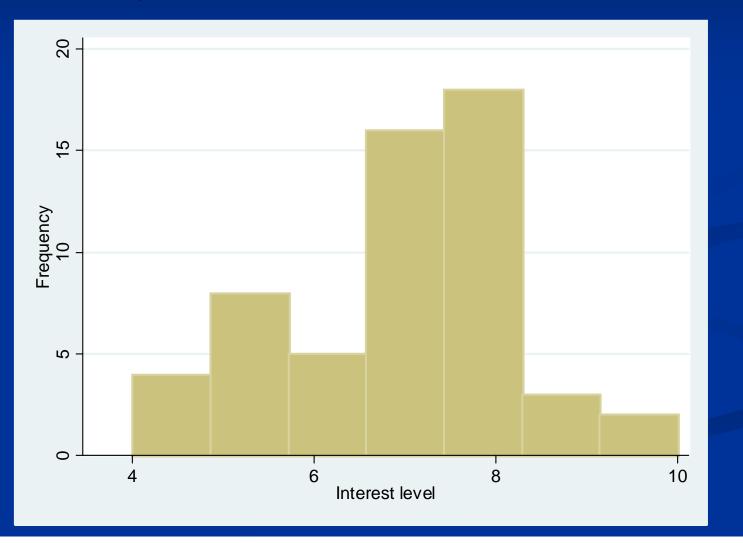
- Histograms: Display the distribution of values depicting the (relative) frequencies of observations within intervals (usually of equal size).
- **Boxplots**: Display important summaries of the distribution of values (discuss later).

# Histograms

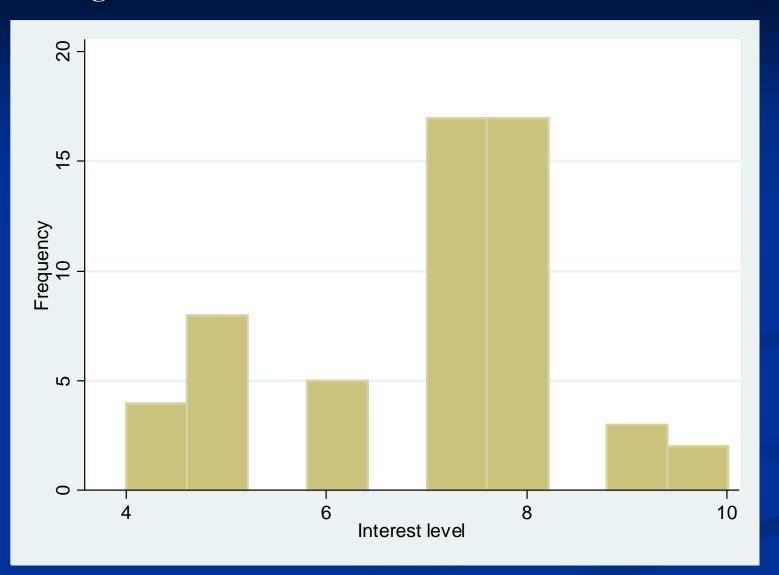
- A histogram does the following:
  - 1. Breaks the range of values into intervals of equal length.
  - 2. Displays the count/percentage of observations that fall into each interval (or "bin").
- Note that the number of intervals and interval width are important and can change the way the histogram looks dramatically for the same set of data.

# Example: Interest

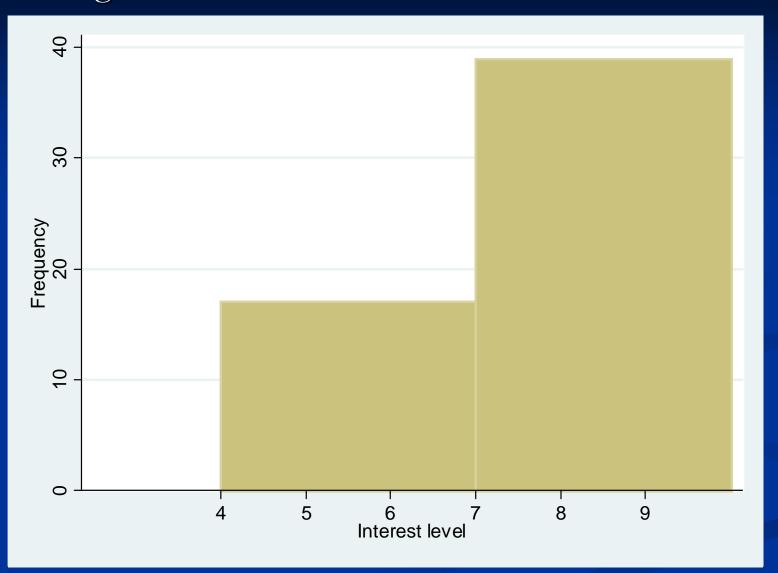
What is your interest in this course?

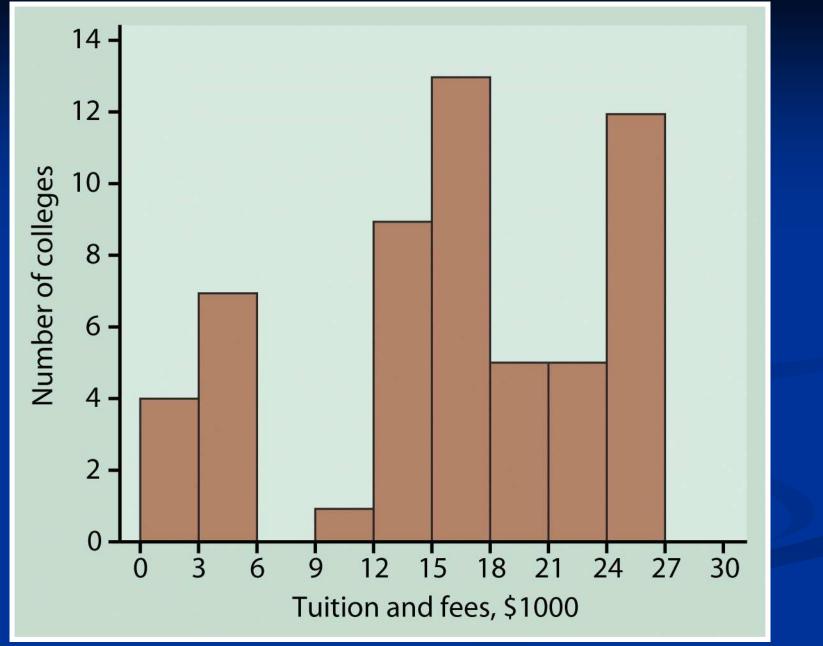


#### Histogram – interest level from MA231

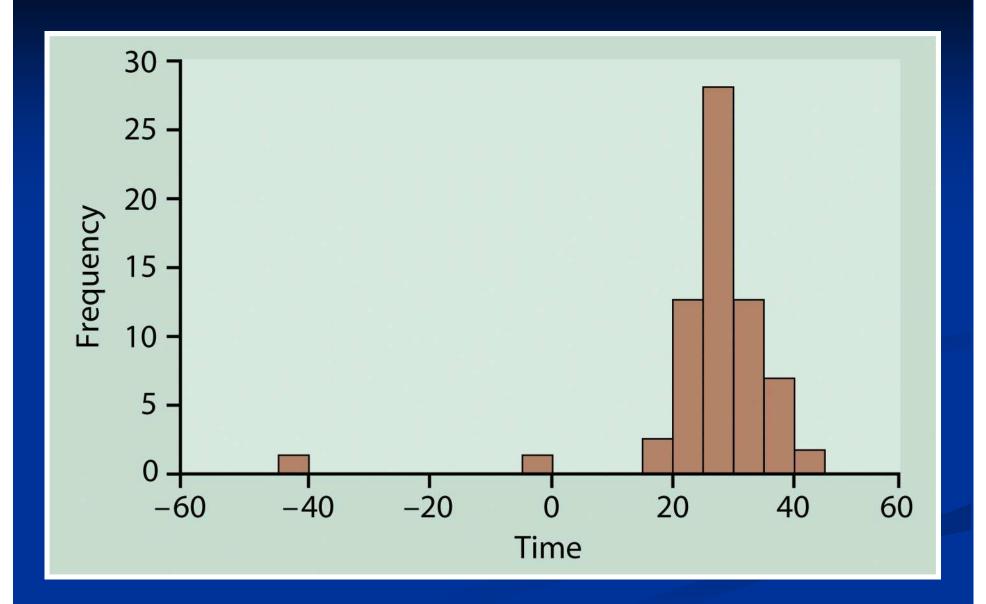


### Histogram – interest level from MA231





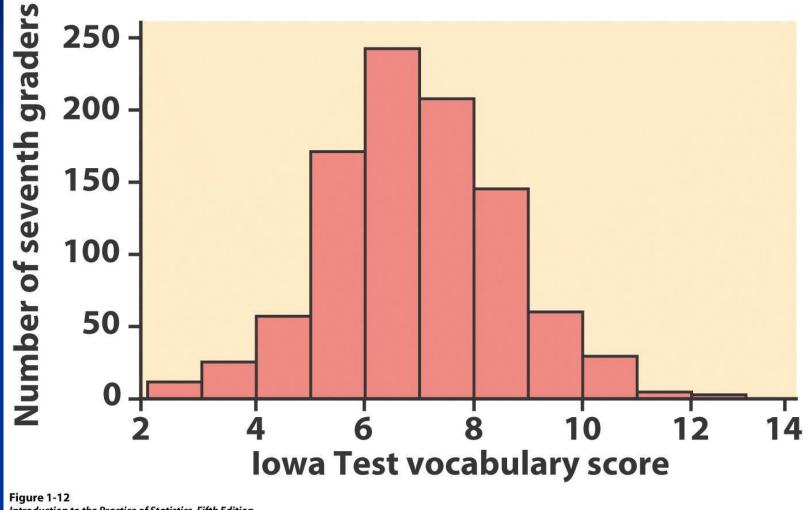
| TABLE 1.1 | Newcon | nb′s measurem | ents of the p | oassage time o | of light |
|-----------|--------|---------------|---------------|----------------|----------|
| 28        | 22     | 36            | 26            | 28             | 28       |
| 26        | 24     | 32            | 30            | 27             | 24       |
| 33        | 21     | 36            | 32            | 31             | 25       |
| 24        | 25     | 28            | 36            | 27             | 32       |
| 34        | 30     | 25            | 26            | 26             | 25       |
| -44       | 23     | 21            | 30            | 33             | 29       |
| 27        | 29     | 28            | 22            | 26             | 27       |
| 16        | 31     | 29            | 36            | 32             | 28       |
| 40        | 19     | 37            | 23            | 32             | 29       |
| -2        | 24     | 25            | 27            | 24             | 16       |
| 29        | 20     | 28            | 27            | 39             | 23       |



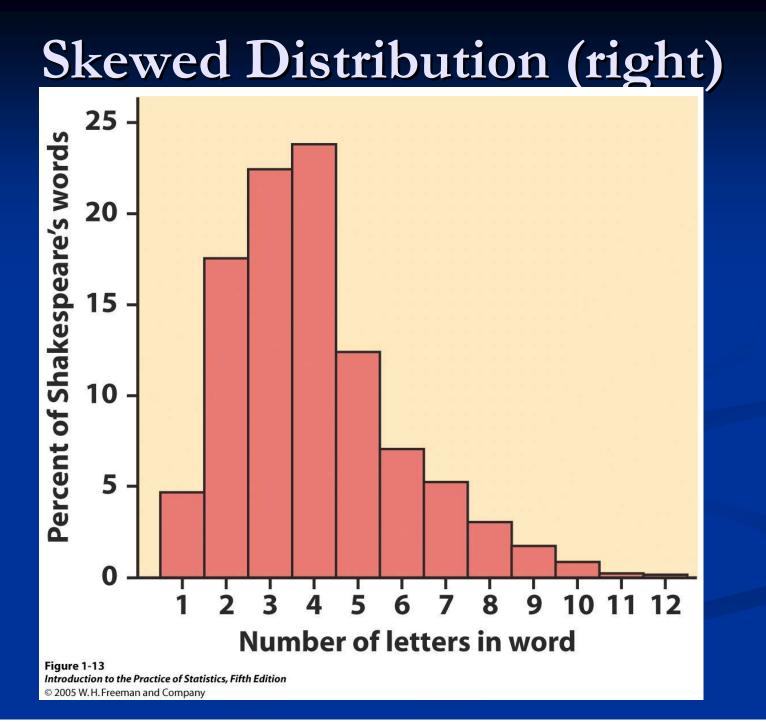
# Shape

- The shape of the distribution can be described by visually inspecting it.
- We generally say it is either symmetric or skewed.
- If it is skewed, it can be skewed right or left.
- We also can state how many peaks it has (one peak = unimodal)

# Symmetric Distributions



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# **Stem-and-Leaf Plots**

#### STEMPLOT

#### To make a **stemplot**:

**1.** Separate each observation into a **stem** consisting of all but the final (rightmost) digit and a **leaf**, the final digit. Stems may have as many digits as needed, but each leaf contains only a single digit.

**2.** Write the stems in a vertical column with the smallest at the top, and draw a vertical line at the right of this column.

**3.** Write each leaf in the row to the right of its stem, in increasing order out from the stem.

Definition, pg 11 Introduction to the Practice of Statistics, Fifth Edition © 2005 W. H. Freeman and Company

#### TABLE 1.2

#### Literacy rates (percent) in Islamic nations

| Country    | Female<br>percent | Male<br>percent | Country      | Female<br>percent | Male<br>percent |
|------------|-------------------|-----------------|--------------|-------------------|-----------------|
| Algeria    | 60                | 78              | Morocco      | 38                | 68              |
| Bangladesh | 31                | 50              | Saudi Arabia | 70                | 84              |
| Egypt      | 46                | 68              | Syria        | 63                | 89              |
| Iran       | 71                | 85              | Tajikistan   | 99                | 100             |
| Jordan     | 86                | 96              | Tunisia      | 63                | 83              |
| Kazakhstan | 99                | 100             | Turkey       | 78                | 94              |
| Lebanon    | 82                | 95              | Uzbekistan   | 99                | 100             |
| Libya      | 71                | 92              | Yemen        | 29                | 70              |
| Malaysia   | 85                | 92              |              |                   |                 |

Table 1-2Introduction to the Practice of Statistics, Fifth Edition© 2005 W.H. Freeman and Company

| 2   | 2 | 9    | 2 | 9    |  |
|-----|---|------|---|------|--|
| 3   | 3 | 18   | 3 | 18   |  |
| 4   | 4 | 6    | 4 | 6    |  |
| 5   | 5 |      | 5 |      |  |
| 6   | 6 | 033  | 6 | 033  |  |
| 7   | 7 | 1108 | 7 | 0118 |  |
| 8   | 8 | 625  | 8 | 256  |  |
| 9   | 9 | 999  | 9 | 999  |  |
| (a) |   | (b)  |   | (c)  |  |
|     |   |      |   |      |  |

Figure 1-3 Introduction to the Practice of Statistics, Fifth Edition © 2005 W.H.Freeman and Company